Package: predint (via r-universe)

September 17, 2024

Type Package Title Prediction Intervals Version 2.2.1.9000 Description An implementation of prediction intervals for overdispersed count data, for overdispersed binomial data and for linear random effects models. License GPL $(>= 2)$ Encoding UTF-8 LazyData true Imports stats, graphics, methods RoxygenNote 7.2.3 **Suggests** rmarkdown, knitr, test that $(>= 3.0.0)$ Config/testthat/edition 3 **Depends** R ($>= 2.10$), ggplot2, lme4, MASS URL <https://github.com/MaxMenssen/predint> BugReports <https://github.com/MaxMenssen/predint/issues> Repository https://maxmenssen.r-universe.dev RemoteUrl https://github.com/maxmenssen/predint RemoteRef HEAD

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```
ames_HCD
```
Historical numbers of revertant colonies in the Ames test (OECD 471)

Description

This data set contains artificial historical control data that was sampled in order to mimic the number of revertant colonies based on two or three petri dishes.

Usage

ames_HCD

Format

A data.frame with 2 rows and 10 columns:

rev_col no. of revertant colonies

no_dish no. of petri dishes in the control group

as.data.frame.predint *Store prediction intervals or limits as a* data.frame

Description

Get the prediction intervals or limits of an object of class predint and save them as a data. frame.

Usage

S3 method for class 'predint' as.data.frame(x, ...)

Arguments

Value

This function returns the prediction intervals or limits stored in an object of class "predint" as a data.frame

Examples

```
### PI for quasi-Poisson data
pred_int <- quasi_pois_pi(histdat=ames_HCD,
                          newoffset=3,
                          nboot=100,
                          traceplot = FALSE)
```

```
# Return the prediction intervals as a data.frame
as.data.frame(pred_int)
```
Please note that nboot was set to 100 in order to decrease computing time # of the example. For a valid analysis set nboot=10000.

This data set contains sampled beta-binomial data from 10 clusters each of size 50. The data set was sampled with rbbinom(n=10, size=50, prob=0.1, rho=0.06).

Usage

bb_dat1

Format

A data.frame with 10 rows and 2 columns:

succ number of successes

fail number of failures

bb_dat2 *Beta-binomial data (example 2)*

Description

This data set contains sampled beta-binomial data from 3 clusters each of different size. The data set was sampled with rbbinom(n=3, size=c(40, 50, 60), prob=0.1, rho=0.06).

Usage

bb_dat2

Format

A data.frame with 3 rows and 2 columns:

succ number of successes

fail number of failures

bb_pi() is a helper function that is internally called by beta_bin_pi(). It calculates simple uncalibrated prediction intervals for binary data with overdispersion changing between the clusters (beta-binomial).

Usage

```
bb_pi(
  newsize,
 histsize,
 pi,
  rho,
  q = qnorm(1 - 0.05/2),
  alternative = "both",
  newdat = NULL,histdat = NULL,
  algorithm = NULL
)
```
Arguments

Details

This function returns a simple uncalibrated prediction interval

$$
[l, u]_m = n_m^* \hat{\pi} \pm q \sqrt{n_m^* \hat{\pi} (1 - \hat{\pi}) [1 + (n_m^* - 1)\hat{\rho}] + \left[\frac{n_m^* \hat{\pi} (1 - \hat{\pi})}{\sum_h n_h} + \frac{\sum_h n_h - 1}{\sum_h n_h} n_m^* \hat{\pi} (1 - \hat{\pi})\hat{\rho} \right]}
$$

with n_m^* as the number of experimental units in the $m = 1, 2, ..., M$ future clusters, $\hat{\pi}$ as the estimate for the binomial proportion obtained from the historical data, $\hat{\rho}$ as the estimate for the intra class correlation and n_h as the number of experimental units per historical cluster.

The direct application of this uncalibrated prediction interval to real life data is not recommended. Please use beta_bin_pi() for real life applications.

Value

bb_pi() returns an object of class c("predint", "betaBinomialPI") with prediction intervals or limits in the first entry (\$prediction).

Examples

```
# Pointwise uncalibrated PI
bb_pred <- bb_pi(newsize=c(50), pi=0.3, rho=0.05, histsize=rep(50, 20), q=qnorm(1-0.05/2))
summary(bb_pred)
```

```
beta_bin_pi Prediction intervals for beta-binomial data
```
Description

beta_bin_pi() calculates bootstrap calibrated prediction intervals for beta-binomial data

Usage

```
beta_bin_pi(
  histdat,
  newdat = NULL,newsize = NULL,
  alternative = "both",
  alpha = 0.05,
  nboot = 10000,delt<sub>1</sub>min = 0.01,
  delta_max = 10,
  tolerance = 0.001,traceplot = TRUE,
  n_bisec = 30,
  algorithm = "MS22mod"
)
```
beta_bin_pi 7

Arguments

Details

This function returns bootstrap-calibrated prediction intervals as well as lower or upper prediction limits.

If algorithm is set to "MS22", both limits of the prediction interval are calibrated simultaneously using the algorithm described in Menssen and Schaarschmidt (2022), section 3.2.4. The calibrated prediction interval is given as

$$
[l, u]_m = n_m^* \hat{\pi} \pm q^{calib} \hat{se}(Y_m - y_m^*)
$$

where

$$
\hat{se}(Y_m - y_m^*) = \sqrt{n_m^* \hat{\pi}(1-\hat{\pi})[1+(n_m^*-1)\hat{\rho}]+[\frac{n_m^{*2}\hat{\pi}(1-\hat{\pi})}{\sum_h n_h} + \frac{\sum_h n_h - 1}{\sum_h n_h}n_m^{*2}\hat{\pi}(1-\hat{\pi})\hat{\rho}]}
$$

with n_m^* as the number of experimental units in the future clusters, $\hat{\pi}$ as the estimate for the binomial proportion obtained from the historical data, q^{calib} as the bootstrap-calibrated coefficient, $\hat{\rho}$ as the estimate for the intra class correlation (Lui et al. 2000) and n_h as the number of experimental units per historical cluster.

If algorithm is set to "MS22mod", both limits of the prediction interval are calibrated independently from each other. The resulting prediction interval is given by

$$
[l, u]_m = \left[n_m^* \hat{\pi} - q_l^{calib} \hat{s} e(Y_m - y_m^*), \quad n_m^* \hat{\pi} + q_u^{calib} \hat{s} e(Y_m - y_m^*) \right]
$$

Please note, that this modification does not affect the calibration procedure, if only prediction limits are of interest.

beta_bin_pi returns an object of class c("predint", "betaBinomialPI") with prediction intervals or limits in the first entry (\$prediction).

References

Lui et al. (2000): Confidence intervals for the risk ratio under cluster sampling based on the betabinomial model. Statistics in Medicine.

[doi:10.1002/10970258\(20001115\)19:21<2933::AIDSIM591>3.0.CO;2Q](https://doi.org/10.1002/1097-0258%2820001115%2919%3A21%3C2933%3A%3AAID-SIM591%3E3.0.CO%3B2-Q)

Menssen and Schaarschmidt (2022): Prediction intervals for all of M future observations based on linear random effects models. Statistica Neerlandica. [doi:10.1111/stan.12260](https://doi.org/10.1111/stan.12260)

Examples

```
# Prediction interval
pred_int <- beta_bin_pi(histdat=mortality_HCD, newsize=40, nboot=100)
summary(pred_int)
```

```
# Upper prediction bound
pred_u <- beta_bin_pi(histdat=mortality_HCD, newsize=40, alternative="upper", nboot=100)
summary(pred_u)
```
Please note that nboot was set to 100 in order to decrease computing time # of the example. For a valid analysis set nboot=10000.

Description

This helper function returns a bootstrap calibrated coefficient for the calculation of prediction intervals (and limits).

Usage

```
bisection(
  y_star_hat,
  pred_se,
  y_star,
  alternative,
  quant_min,
  quant_max,
  n_bisec,
  tol,
  alpha,
  traceplot = TRUE
)
```
bisection 9

Arguments

Details

This function is an implementation of the bisection algorithm of Menssen and Schaarschmidt 2022. It returns a calibrated coefficient q^{calib} for the calculation of pointwise and simultaneous prediction intervals

$$
[l, u] = \hat{y}_m^* \pm q^{calib}\hat{se}(Y_m - y_m^*),
$$

lower prediction limits

$$
l = \hat{y}_m^* - q^{calib}\hat{se}(Y_m - y_m^*)
$$

or upper prediction limits

$$
u = \hat{y}_m^* + q^{calib}\hat{se}(Y_m - y_m^*)
$$

that cover all of $m = 1, ..., M$ future observations.

In this notation, \hat{y}_m^* are the expected future observations for each of the m future clusters, q^{calib} is the calibrated coefficient and $\hat{se}(Y_m - y_m^*)$ are the standard errors of the prediction.

Value

This function returns q^{calib} in the equation above.

References

Menssen and Schaarschmidt (2022): Prediction intervals for all of M future observations based on linear random effects models. Statistica Neerlandica. [doi:10.1111/stan.12260](https://doi.org/10.1111/stan.12260)

boot_predint() is a helper function to bootstrap new data from the simple uncalibrated prediction intervals implemented in predint.

Usage

boot_predint(pred_int, nboot)

Arguments

Details

This function only works for binomial and Poisson type data. For the sampling of new data from random effects models see [lmer_bs](#page-12-1).

Value

boot_predint returns an object of class c("predint", "bootstrap") which is a list with two entries: One for bootstrapped historical observations and one for bootstrapped future observations.

Examples

```
# Simple quasi-Poisson PI
test_pi <- qp_pi(histoffset=c(3,3,3,4,5), newoffset=3, lambda=10, phi=3, q=1.96)
# Draw 5 bootstrap samles
test_boot <- boot_predint(pred_int = test_pi, nboot=50)
str(test_boot)
summary(test_boot)
```
Please note that the low number of bootstrap samples was chosen in order to # decrease computing time. For valid analysis draw at least 10000 bootstrap samples.

c2_dat1 contains data that is sampled from a balanced cross-classified design. This data set is used in order to demonstrate the functionality of the l mer_{pi}...() functions.

Usage

c2_dat1

Format

A data.frame with 27 rows and 3 columns:

y_ijk observations

a treatment a

b treatment **b**

c2_dat2 *Cross-classified data (example 2)*

Description

c2_dat2 contains data that was sampled from an unbalanced cross-classified design. This data set is used in order to demonstrate the functionality of the lmer_pi_...() functions.

Usage

c2_dat2

Format

A data.frame with 21 rows and 3 columns:

y_ijk observations

a treatment a

b treatment b

c2_dat3 contains data that was sampled from a balanced cross-classified design. This data set is used in order to demonstrate the functionality of the lmer_pi_...() functions.

Usage

c2_dat3

Format

A data.frame with 8 rows and 3 columns:

y_ijk observations

a treatment a

b treatment **b**

c2_dat4 *Cross-classified data (example 4)*

Description

c2_dat4 contains data that was sampled from an unbalanced cross-classified design. This data set is used in order to demonstrate the functionality of the lmer_pi_...() functions.

Usage

c2_dat4

Format

A data.frame with 6 rows and 3 columns:

- y_ijk observations
- a treatment a
- b treatment b

lmer_bs() draws bootstrap samples based on the estimates for the mean and the variance components drawn from a random effects model fit with $lme4$::lmer(). Contrary to $lme4$::bootMer(), the number of observations for each random factor can vary between the original data set and the bootstrapped data. Random effects in model have to be specified as (1|random effect).

Usage

```
lmer_bs(model, newdat = NULL, futmat_list = NULL, nboot)
```
Arguments

Details

The data sampling is based on a list of design matrices (one for each random factor) that can be obtained if newdat and the model formula are provided to lme4::lFormula(). Hence, each random factor that is part of the initial model must have at least two replicates in newdat. If a random factor in the future data set does not have any replicate, a list that contains design matrices (one for each random factor) can be provided via futmat_list.

Value

A list of length nboot containing the bootstrapped observations.

Examples

```
# loading lme4
library(lme4)
```
Fitting a random effects model based on c2_dat1

```
fit <- lmer(y_ijk^-(1|a)+(1|b)+(1|a:b), c2_dat1)
summary(fit)
```
#--

Using c2_dat2 as newdat

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```
c2_dat2
lmer_bs(model=fit, newdat=c2_dat2, nboot=100)
#----------------------------------------------------------------------------
### Using futmat_list
# c2_dat4 has no replication for b. Hence the list of design matrices can not be
# generated by lme4::lFormula() and have to be provided by hand via futmat_list.
c2_dat4
# Build a list containing the design matrices
fml <- vector(length=4, "list")
names(fml) <- c("a:b", "b", "a", "Residual")
fnl[["a:b"]] \leq marix(nrow=6, ncol=2, data=c(1,1,0,0,0,0,0,0,1,1,1,1))fnl[["b"] <- matrix(nrow=6, ncol=1, data=c(1,1,1,1,1,1))
fnl[["a"]] < - matrix(nrow=6, ncol=2, data=c(1,1,0,0,0,0,0,0,0,1,1,1,1))
fml[["Residual"]] <- diag(6)
fml
lmer_bs(model=fit, futmat_list=fml, nboot=100)
```
lmer_pi *Prediction intervals for future observations based on linear random effects models (DEPRECATED)*

Description

This function is deprecated. Please use $lmer_pi_unstruc()$, $lmer_pi_futvec()$ or $lmer_pi_futmat()$.

Usage

```
lmer_pi(
 model,
 newdat = NULL,m = NULL,
 alternative = "both",
  alpha = 0.05,
 nboot = 10000,
```
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```
lambda\_min = 0.01,
lambda_max = 10,
traceplot = TRUE,
n_bisec = 30
```
Arguments

)

Details

This function returns a bootstrap calibrated prediction interval

$$
[l, u] = \hat{y} \pm q\sqrt{\hat{var}(\hat{y} - y)}
$$

with \hat{y} as the predicted future observation, y as the observed future observations, $\sqrt{v \hat{a} r (\hat{y} - y)}$ as the prediction standard error and q as the bootstrap calibrated coefficient that approximates a quantile of the multivariate t-distribution.

Please note that this function relies on linear random effects models that are fitted with lmer() from the lme4 package. Random effects have to be specified as (1|random_effect).

Value

If newdat is specified: A data.frame that contains the future data, the historical mean (hist_mean), the calibrated coefficient (quant_calib), the prediction standard error (pred_se), the prediction interval (lower and upper) and a statement if the prediction interval covers the future observation (cover).

If m is specified: A data.frame that contains the number of future observations (m) the historical mean (hist mean), the calibrated coefficient (quant calib), the prediction standard error (pred se) and the prediction interval (lower and upper).

If alternative is set to "lower": Lower prediction limits are computed instead of a prediction interval.

If alternative is set to "upper": Upper prediction limits are computed instead of a prediction interval.

If traceplot=TRUE, a graphical overview about the bisection process is given.

Examples

```
# This function is deprecated.
# Please use lmer_pi_unstruc() if you want exactly the same functionality.
# Please use lmer_pi_futmat() or lmer_pi_futvec() if you want to take care
# of the future experimental design
```
lmer_pi_futmat *Prediction intervals for future observations based on linear random effects models*

Description

lmer_pi_futmat() calculates a bootstrap calibrated prediction interval for one or more future observation(s) based on linear random effects models. With this approach, the experimental design of the future data is taken into account (see below).

Usage

```
lmer_pi_futmat(
 model,
  newdat = NULL,futmat_list = NULL,
  alternative = "both",
  alpha = 0.05,
  nboot = 10000,delta\_min = 0.01,
  delta_max = 10,tolerance = 0.001,traceplot = TRUE,
  n_bisec = 30,
  algorithm = "MS22"
)
```
Arguments

Details

This function returns bootstrap-calibrated prediction intervals as well as lower or upper prediction limits.

If algorithm is set to "MS22", both limits of the prediction interval are calibrated simultaneously using the algorithm described in Menssen and Schaarschmidt (2022), section 3.2.4. The calibrated prediction interval is given as

$$
[l, u] = \hat{\mu} \pm q^{calib} \sqrt{\widehat{var}(\hat{\mu}) + \sum_{c=1}^{C+1} \hat{\sigma}_c^2}
$$

with $\hat{\mu}$ as the expected future observation (historical mean) and $\hat{\sigma}_c^2$ as the $c = 1, 2, ..., C$ variance components and $\hat{\sigma}_{C+1}^2$ as the residual variance obtained from the random effects model fitted with lme4:: lmer() and q^{calib} as the as the bootstrap-calibrated coefficient used for interval calculation.

If algorithm is set to "MS22mod", both limits of the prediction interval are calibrated independently from each other. The resulting prediction interval is given by

$$
[l, u] = \left[\hat{\mu} - q_l^{calib}\sqrt{\widehat{var}(\hat{\mu}) + \sum_{c=1}^{C+1}\hat{\sigma}_c^2}, \quad \hat{\mu} + q_u^{calib}\sqrt{\widehat{var}(\hat{\mu}) + \sum_{c=1}^{C+1}\hat{\sigma}_c^2}\right].
$$

Please note, that this modification does not affect the calibration procedure, if only prediction limits are of interest.

If newdat is defined, the bootstrapped future observations used for the calibration process mimic the structure of the data set provided via newdat. The data sampling is based on a list of design matrices (one for each random factor) that can be obtained if newdat and the model formula are provided to lme4::lFormula(). Hence, each random factor that is part of the initial model must have at least two replicates in newdat.

If a random factor in the future data set does not have any replicate, a list that contains design matrices (one for each random factor) can be provided via futmat_list.

This function is an implementation of the PI given in Menssen and Schaarschmidt 2022 section 3.2.4, except, that the bootstrap calibration values are drawn from bootstrap samples that mimic the future data as described above.

Value

lmer_pi_futmat() returns an object of class c("predint", "normalPI") with prediction intervals or limits in the first entry (\$prediction).

References

Menssen and Schaarschmidt (2022): Prediction intervals for all of M future observations based on linear random effects models. Statistica Neerlandica, [doi:10.1111/stan.12260](https://doi.org/10.1111/stan.12260)

Examples

```
# loading lme4
library(lme4)
# Fitting a random effects model based on c2_dat1
fit <- lmer(y_ijk^-(1|a)+(1|b)+(1|a:b), c2_dat1)
summary(fit)
#----------------------------------------------------------------------------
### Using newdat
# Prediction interval using c2_dat2 as future data
pred_int <- lmer_pi_futmat(model=fit, newdat=c2_dat2, alternative="both", nboot=100)
summary(pred_int)
# Upper prediction limit for m=1 future observations
pred_u <- lmer_pi_futmat(model=fit, newdat=1, alternative="upper", nboot=100)
summary(pred_u)
#----------------------------------------------------------------------------
### Using futmat_list
# c2_dat4 has no replication for b. Hence the list of design matrices can not be
# generated by lme4::lFormula() and have to be provided by hand via futmat_list.
c2_dat4
# Build a list containing the design matrices
fml <- vector(length=4, "list")
names(fml) <- c("a:b", "b", "a", "Residual")
fnl[["a:b"] <- matrix(nrow=6, ncol=2, data=c(1,1,0,0,0,0,0,0,0,1,1,1,1))
fml[["b"] <- matrix(nrow=6, ncol=1, data=c(1,1,1,1,1,1))
fnl[["a"]] < - matrix(nrow=6, ncol=2, data=c(1,1,0,0,0,0, 0,0,1,1,1,1))
fml[["Residual"]] <- diag(6)
fml
# Please note, that the design matrix for the interaction term a:b is also
```
provided even there is no replication for b, since it is assumed that

both, the historical and the future data descent from the same data generating

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```
# process.
# Calculate the PI
pred_fml <- lmer_pi_futmat(model=fit, futmat_list=fml, alternative="both", nboot=100)
summary(pred_fml)
#----------------------------------------------------------------------------
# Please note that nboot was set to 100 in order to decrease computing time
# of the example. For a valid analysis set nboot=10000.
```
lmer_pi_futvec *Prediction intervals for future observations based on linear random effects models*

Description

lmer_pi_futvec() calculates a bootstrap calibrated prediction interval for one or more future observation(s) based on linear random effects models. With this approach, the experimental design of the future data is taken into account (see below).

Usage

```
lmer_pi_futvec(
 model,
  futvec,
  newdat = NULL,alternative = "both",
  alpha = 0.05,
  nboot = 10000,delta\_min = 0.01,
  delta_max = 10,tolerance = 0.001,traceplot = TRUE,
  n_bisec = 30,
  algorithm = "MS22"
```

```
\mathcal{L}
```
Arguments

Details

This function returns bootstrap-calibrated prediction intervals as well as lower or upper prediction limits.

If algorithm is set to "MS22", both limits of the prediction interval are calibrated simultaneously using the algorithm described in Menssen and Schaarschmidt (2022), section 3.2.4. The calibrated prediction interval is given as

$$
[l, u] = \hat{\mu} \pm q^{calib} \sqrt{\widehat{var}(\hat{\mu}) + \sum_{c=1}^{C+1} \hat{\sigma}_c^2}
$$

with $\hat{\mu}$ as the expected future observation (historical mean) and $\hat{\sigma}_c^2$ as the $c = 1, 2, ..., C$ variance components and $\hat{\sigma}_{C+1}^2$ as the residual variance obtained from the random effects model fitted with lme4:: lmer() and q^{calib} as the as the bootstrap-calibrated coefficient used for interval calculation.

If algorithm is set to "MS22mod", both limits of the prediction interval are calibrated independently from each other. The resulting prediction interval is given by

$$
[l,u]=\Big[\hat{\mu}-q_l^{calib}\sqrt{\widehat{var}(\hat{\mu})+\sum_{c=1}^{C+1}\hat{\sigma}_c^2},\quad \hat{\mu}+q_u^{calib}\sqrt{\widehat{var}(\hat{\mu})+\sum_{c=1}^{C+1}\hat{\sigma}_c^2}\Big].
$$

Please note, that this modification does not affect the calibration procedure, if only prediction limits are of interest.

Be aware that the sampling structure of the historical data must contain the structure of the future data. This means that the observations per random factor must be less or equal in the future data compared to the historical data.

This function is an implementation of the PI given in Menssen and Schaarschmidt 2022 section 3.2.4 except that the bootstrap calibration values are drawn from bootstrap samples that mimic the future data.

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Value

lmer_pi_futvec() returns an object of class c("predint", "normalPI") with prediction intervals or limits in the first entry (\$prediction).

References

Menssen and Schaarschmidt (2022): Prediction intervals for all of M future observations based on linear random effects models. Statistica Neerlandica, [doi:10.1111/stan.12260](https://doi.org/10.1111/stan.12260)

Examples

```
# loading lme4
library(lme4)
# Fitting a random effects model based on c2_dat1
fit <- lmer(y_ijk^-(1|a)+(1|b)+(1|a:b), c2_dat1)
summary(fit)
#----------------------------------------------------------------------------
### Prediction interval using c2_dat3 as future data
# without printing c2_dat3 in the output
# Row numbers of the historical data c2_dat1 that define the structure of
# the future data c2_dat3
futvec <- c(1, 2, 4, 5, 10, 11, 13, 14)
# Calculating the PI
pred_int <- lmer_pi_futvec(model=fit, futvec=futvec, nboot=100)
summary(pred_int)
#----------------------------------------------------------------------------
### Calculating the PI with c2_dat3 printed in the output
pred_int_new <- lmer_pi_futvec(model=fit, futvec=futvec, newdat=c2_dat3, nboot=100)
summary(pred_int_new)
#----------------------------------------------------------------------------
### Upper prediction limit for m=1 future observation
pred_u <- lmer_pi_futvec(model=fit, futvec=1, alternative="upper", nboot=100)
summary(pred_u)
#----------------------------------------------------------------------------
```
Please note that nboot was set to 100 in order to decrease computing time # of the example. For a valid analysis set nboot=10000.

lmer_pi_unstruc *Prediction intervals for future observations based on linear random effects models*

Description

lmer_pi_unstruc() calculates a bootstrap calibrated prediction interval for one or more future observation(s) based on linear random effects models as described in section 3.2.4. of Menssen and Schaarschmidt (2022). Please note, that the bootstrap calibration used here does not consider the sampling structure of the future data, since the calibration values are drawn randomly from bootstrap data sets that have the same structure as the historical data.

Usage

```
lmer_pi_unstruc(
 model,
 newdat = NULL,m = NULL,alternative = "both",
 alpha = 0.05,
 nboot = 10000,delt=min = 0.01,
 delta_max = 10,tolerance = 0.001,traceplot = TRUE,
 n_bisec = 30,
  algorithm = "MS22"
)
```
Arguments

Details

This function returns bootstrap-calibrated prediction intervals as well as lower or upper prediction limits.

If algorithm is set to "MS22", both limits of the prediction interval are calibrated simultaneously using the algorithm described in Menssen and Schaarschmidt (2022), section 3.2.4. The calibrated prediction interval is given as

$$
[l, u] = \hat{\mu} \pm q^{calib} \sqrt{\widehat{var}(\hat{\mu}) + \sum_{c=1}^{C+1} \hat{\sigma}_c^2}
$$

with $\hat{\mu}$ as the expected future observation (historical mean) and $\hat{\sigma}_c^2$ as the $c = 1, 2, ..., C$ variance components and $\hat{\sigma}_{C+1}^2$ as the residual variance obtained from the random effects model fitted with lme4:: lmer() and q^{calib} as the as the bootstrap-calibrated coefficient used for interval calculation.

If algorithm is set to "MS22mod", both limits of the prediction interval are calibrated independently from each other. The resulting prediction interval is given by

$$
[l, u] = \left[\hat{\mu} - q_l^{calib}\sqrt{\widehat{var}(\hat{\mu}) + \sum_{c=1}^{C+1}\hat{\sigma}_c^2}, \quad \hat{\mu} + q_u^{calib}\sqrt{\widehat{var}(\hat{\mu}) + \sum_{c=1}^{C+1}\hat{\sigma}_c^2}\right].
$$

Please note, that this modification does not affect the calibration procedure, if only prediction limits are of interest.

This function is an direct implementation of the PI given in Menssen and Schaarschmidt 2022 section 3.2.4.

Value

lmer_pi_futvec() returns an object of class c("predint", "normalPI") with prediction intervals or limits in the first entry (\$prediction).

References

Menssen and Schaarschmidt (2022): Prediction intervals for all of M future observations based on linear random effects models. Statistica Neerlandica, [doi:10.1111/stan.12260](https://doi.org/10.1111/stan.12260)

Examples

```
# loading lme4
library(lme4)
# Fitting a random effects model based on c2_dat1
fit <- lmer(y_ijk^-(1|a)+(1|b)+(1|a:b), c2_data1)summary(fit)
```
Prediction interval using c2_dat2 as future data

```
pred_int <- lmer_pi_unstruc(model=fit, newdat=c2_dat2, alternative="both", nboot=100)
summary(pred_int)
# Upper prediction limit for m=3 future observations
pred_u <- lmer_pi_unstruc(model=fit, m=3, alternative="upper", nboot=100)
summary(pred_u)
# Please note that nboot was set to 100 in order to decrease computing time
# of the example. For a valid analysis set nboot=10000.
```
mortality_HCD *Historical mortality of male B6C3F1-mice*

Description

This data set contains historical control data about the mortality of male B6C3F1-mice obtained in long term carcinogenicity studies at the National Toxicology Program presented in NTP Historical Control Reports from 2013 to 2016. It was used in Menssen and Schaarschmidt 2019 as a real life example.

Usage

mortality_HCD

Format

A data.frame with 2 rows and 10 columns:

dead no. of dead mice

alive no. of living mice

References

Menssen and Schaarschmidt (2019): Prediction intervals for overdispersed binomial data with application to historical controls. Statistics in Medicine. [doi:10.1002/sim.8124](https://doi.org/10.1002/sim.8124) NTP Historical Control Reports: <https://ntp.niehs.nih.gov/data/controls>

nb_pi() is a helper function that is internally called by neg_bin_pi(). It calculates simple uncalibrated prediction intervals for negative-binomial data with offsets.

Usage

```
nb_pi(
 newoffset,
 histoffset,
  lambda,
 kappa,
  q = qnorm(1 - 0.05/2),
 alternative = "both",
  newdat = NULL,histdat = NULL,
  algorithm = NULL
)
```
Arguments

Details

This function returns a simple uncalibrated prediction interval

$$
[l,u]_m=n_m^*\hat{\lambda}\pm q\sqrt{n_m^*\frac{\hat{\lambda}+\hat{\kappa}\bar{n}\hat{\lambda}}{\bar{n}H}+(n_m^*\hat{\lambda}+\hat{\kappa}n_m^{*2}\hat{\lambda}^2)}
$$

with n_m^* as the number of experimental units in $m = 1, 2, ..., M$ future clusters, $\hat{\lambda}$ as the estimate for the Poisson mean obtained from the historical data, $\hat{\kappa}$ as the estimate for the dispersion parameter, n_h as the number of experimental units per historical cluster and $\bar{n} = \sum_h^{n_h} n_h / H$.

The direct application of this uncalibrated prediction interval to real life data is not recommended. Please use the neg_bin_pi() function for real life applications.

Value

```
np_pi returns an object of class c("predint", "negativeBinomialPI").
```
Examples

```
# Prediction interval
nb_pred <- nb_pi(newoffset=3, lambda=3, kappa=0.04, histoffset=1:9, q=qnorm(1-0.05/2))
summary(nb_pred)
```
neg_bin_pi *Prediction intervals for negative-binomial data*

Description

neg_bin_pi() calculates bootstrap calibrated prediction intervals for negative-binomial data.

Usage

```
neg_bin_pi(
 histdat,
  newdat = NULL,newoffset = NULL,
  alternative = "both",
  alpha = 0.05,
  nboot = 10000,delta_min = 0.01,
  delta_max = 10,tolerance = 0.001,traceplot = TRUE,
  n_bisec = 30,
  algorithm = "MS22mod"
\mathcal{L}
```
Arguments

histdat a data.frame with two columns. The first has to contain the historical observations. The second has to contain the number of experimental units per study (offsets).

neg_bin_pi 27

Details

This function returns bootstrap-calibrated prediction intervals as well as lower or upper prediction limits.

If algorithm is set to "MS22", both limits of the prediction interval are calibrated simultaneously using the algorithm described in Menssen and Schaarschmidt (2022), section 3.2.4. The calibrated prediction interval is given as

$$
[l,u]_m=n_m^*\hat\lambda\pm q\sqrt{n_m^*\frac{\hat\lambda+\hat\kappa\bar n\hat\lambda}{\bar nH}+(n_m^*\hat\lambda+\hat\kappa n_m^{*2}\hat\lambda^2)}
$$

with n_m^* as the number of experimental units in the future clusters, $\hat{\lambda}$ as the estimate for the Poisson mean obtained from the historical data, $\hat{\kappa}$ as the estimate for the dispersion parameter, n_h as the number of experimental units per historical cluster and $\bar{n} = \sum_{h}^{n_h} n_h / H$.

If algorithm is set to "MS22mod", both limits of the prediction interval are calibrated independently from each other. The resulting prediction interval is given by

$$
[l,u]=\Big[n_m^*\hat{\lambda}-q_l^{calib}\sqrt{n_m^*\frac{\hat{\lambda}+\hat{\kappa}\bar{n}\hat{\lambda}}{\bar{n}H}+(n_m^*\hat{\lambda}+\hat{\kappa}n_m^{*2}\hat{\lambda}^2)}, \quad n_m^*\hat{\lambda}+q_u^{calib}\sqrt{n_m^*\frac{\hat{\lambda}+\hat{\kappa}\bar{n}\hat{\lambda}}{\bar{n}H}+(n_m^*\hat{\lambda}+\hat{\kappa}n_m^{*2}\hat{\lambda}^2)}\Big]
$$

Please note, that this modification does not affect the calibration procedure, if only prediction limits are of interest.

Value

neg_bin_pi() returns an object of class c("predint", "negativeBinomialPI") with prediction intervals or limits in the first entry (\$prediction).

References

Menssen and Schaarschmidt (2022): Prediction intervals for all of M future observations based on linear random effects models. Statistica Neerlandica, [doi:10.1111/stan.12260](https://doi.org/10.1111/stan.12260)

Examples

```
# HCD from the Ames test
ames_HCD
# Prediction interval for one future number of revertant colonies
# obtained in three petridishes
pred_int <- neg_bin_pi(histdat=ames_HCD, newoffset=3, nboot=100)
summary(pred_int)
# Please note that nboot was set to 100 in order to decrease computing time
```

```
# of the example. For a valid analysis set nboot=10000.
```
normal_pi *Simple uncalibrated prediction intervals for normal distributed data*

Description

normal_pi() is a helper function that is internally called by the $lmer_pi$...() functions. It calculates simple uncalibrated prediction intervals for normal distributed observations.

Usage

```
normal_pi(
 mu,
 pred_se,
 m = 1,
  q = qnorm(1 - 0.05/2),
  alternative = "both",
  futmat_list = NULL,
  futvec = NULL,newdat = NULL,histdat = NULL,
  algorithm = NULL
)
```
Arguments

normal_pi 29

Details

This function returns a simple uncalibrated prediction interval as given in Menssen and Schaarschmidt 2022

$$
[l, u] = \hat{\mu} \pm q \sqrt{\widehat{var}(\hat{\mu}) + \sum_{c=1}^{C+1} \hat{\sigma}_c^2}
$$

with $\hat{\mu}$ as the expected future observation (historical mean) and $\hat{\sigma}_c^2$ as the $c = 1, 2, ..., C$ variance components and $\hat{\sigma}_{C+1}^2$ as the residual variance and q as the quantile used for interval calculation.

The direct application of this uncalibrated prediction interval to real life data is not recommended. Please use the $lmer_pi$...() functions for real life applications.

Value

normal_pi() returns an object of class c("predint", "normalPI") with prediction intervals or limits in the first entry (\$prediction).

References

Menssen and Schaarschmidt (2022): Prediction intervals for all of M future observations based on linear random effects models. Statistica Neerlandica, [doi:10.1111/stan.12260](https://doi.org/10.1111/stan.12260)

Examples

```
# simple PI
norm_pred <- normal_pi(mu=10, pred_se=3, m=1)
summary(norm_pred)
```
pi_rho_est() estimates the overall binomial proportion $\hat{\pi}$ and the intra class correlation $\hat{\rho}$ of data that is assumed to follow the beta-binomial distribution. The estimation of $\hat{\pi}$ and $\hat{\rho}$ is done following the approach of Lui et al. 2000.

Usage

pi_rho_est(dat)

Arguments

dat a data.frame with two columns (successes and failures)

Value

a vector containing estimates for π and ρ

References

Lui, K.-J., Mayer, J.A. and Eckhardt, L: Confidence intervals for the risk ratio under cluster sampling based on the beta-binomial model. Statistics in Medicine.2000;19:2933-2942. [doi:10.1002/](https://doi.org/10.1002/1097-0258%2820001115%2919%3A21%3C2933%3A%3AAID-SIM591%3E3.0.CO%3B2-Q) [10970258\(20001115\)19:21<2933::AIDSIM591>3.0.CO;2Q](https://doi.org/10.1002/1097-0258%2820001115%2919%3A21%3C2933%3A%3AAID-SIM591%3E3.0.CO%3B2-Q)

Examples

```
# Estimates for bb_dat1
pi_rho_est(bb_dat1)
```
plot.predint *Plots of* predint *objects*

Description

This function provides methodology for plotting the prediction intervals or limits that are calculated using the functionality of the predint package.

Usage

```
## S3 method for class 'predint'
plot(x, ..., size = 4, width = 0.05, alpha = 0.5)
```
print.predint 31

Arguments

Value

```
Since plot.predint() is based on ggplot2::ggplot, it returns an object of class c("gg", "ggplot").
```
Examples

```
### PI for quasi-Poisson data
pred_int <- quasi_pois_pi(histdat=ames_HCD,
                          newoffset=3,
                          nboot=100,
                          traceplot = FALSE)
### Plot the PI
plot(pred_int)
### Since plot.predint is based on ggplot, the grafic can be altered using
# the methodology provided via ggplot2
plot(pred_int)+
    theme_classic()
```
print.predint *Print objects of class* predint

Description

Print objects of class predint

Usage

```
## S3 method for class 'predint'
print(x, \ldots)
```
Arguments

Value

prints output to the console

This data set contains sampled quasi-binomial data from 10 clusters each of size 50. The data set was sampled with rqbinom(n=10, size=50, prob=0.1, phi=3).

Usage

qb_dat1

Format

A data.frame with 3 rows and 2 columns:

succ numbers of success

fail numbers of failures

qb_dat2 *Quasi-binomial data (example 2)*

Description

This data set contains sampled quasi binomial data from 3 clusters with different size.The data set was sampled with rqbinom(n=3, size=c(40, 50, 60), prob=0.1, phi=3).

Usage

qb_dat2

Format

A data.frame with 3 rows and 2 columns:

succ numbers of success

fail numbers of failures

qb_pi() is a helper function that is internally called by quasi_bin_pi(). It calculates simple uncalibrated prediction intervals for binary data with constant overdispersion (quasi-binomial assumption).

Usage

```
qb_pi(
  newsize,
 histsize,
 pi,
 phi,
  q = qnorm(1 - 0.05/2),
  alternative = "both",
  newdat = NULL,histdat = NULL,
  algorithm = NULL
)
```
Arguments

Details

This function returns a simple uncalibrated prediction interval

$$
[l, u]_m = n_m^* \hat{\pi} \pm q \sqrt{\hat{\phi} n_m^* \hat{\pi} (1 - \hat{\pi}) + \frac{\hat{\phi} n_m^{*2} \hat{\pi} (1 - \hat{\pi})}{\sum_h n_h}}
$$

with n_m^* as the number of experimental units in the $m = 1, 2, ..., M$ future clusters, $\hat{\pi}$ as the estimate for the binomial proportion obtained from the historical data, $\hat{\phi}$ as the estimate for the dispersion parameter and n_h as the number of experimental units per historical cluster.

The direct application of this uncalibrated prediction interval to real life data is not recommended. Please use the beta_bin_pi() functions for real life applications.

Value

```
qb_pi returns an object of class c("predint", "quasiBinomailPI").
```
Examples

```
qb_pred <- qb_pi(newsize=50, pi=0.3, phi=3, histsize=c(50, 50, 30), q=qnorm(1-0.05/2))
summary(qb_pred)
```
qp_dat1 *Quasi-Poisson data (example 1)*

Description

This data set contains sampled quasi-Poisson data for 10 clusters. The data set was sampled with rqpois(n=10, lambda=50, phi=3).

Usage

qp_dat1

Format

A data.frame with two columns

y numbers of eventzs

offset size of experimental units

This data set contains sampled quasi-Poisson data for 3 clusters. The data set was sampled with rqpois(n=3, lambda=50, phi=3).

Usage

qp_dat2

Format

A data.frame with two columns

y numbers of eventzs

offset size of experimental units

qp_pi *Simple uncalibrated prediction intervals for quasi-Poisson data*

Description

 $qppi()$ is a helper function that is internally called by quasi_pois_pi(). It calculates simple uncalibrated prediction intervals for Poisson data with constant overdispersion (quasi-Poisson assumption).

Usage

```
qp_pi(
  newoffset,
 histoffset,
  lambda,
 phi,
  q = qnorm(1 - 0.05/2),
  alternative = "both",
  newdat = NULL,histdat = NULL,
  algorithm = NULL
)
```
Arguments

Details

This function returns a simple uncalibrated prediction interval

$$
[l,u]_m = n_m^* \hat{\lambda} \pm q \sqrt{n_m^* \hat{\phi} \hat{\lambda} + \frac{n_m^{*2} \hat{\phi} \hat{\lambda}}{\sum_h n_h}}
$$

with n_m^* as the number of experimental units in the $m = 1, 2, ..., M$ future clusters, $\hat{\lambda}$ as the estimate for the Poisson mean obtained from the historical data, $\hat{\phi}$ as the estimate for the dispersion parameter and n_h as the number of experimental units per historical cluster.

The direct application of this uncalibrated prediction interval to real life data is not recommended. Please use the quasi_pois_pi_pi() functions for real life applications.

Value

qp_pi returns an object of class c("predint", "quasiPoissonPI").

Examples

```
# Prediction interval
qp_pred <- qp_pi(newoffset=3, lambda=3, phi=3, histoffset=1:9, q=qnorm(1-0.05/2))
summary(qp_pred)
```


quasi_bin_pi() calculates bootstrap calibrated prediction intervals for binomial data with constant overdispersion (quasi-binomial assumption).

Usage

```
quasi_bin_pi(
 histdat,
 newdat = NULL,newsize = NULL,
  alternative = "both",
  alpha = 0.05,
 nboot = 10000,
  delt<sub>1</sub>min = 0.01,
  delta_max = 10,tolerance = 0.001,
  traceplot = TRUE,
  n_bisec = 30,
  algorithm = "MS22mod"
)
```
Arguments

Details

This function returns bootstrap-calibrated prediction intervals as well as lower or upper prediction limits.

If algorithm is set to "MS22", both limits of the prediction interval are calibrated simultaneously using the algorithm described in Menssen and Schaarschmidt (2022), section 3.2.4. The calibrated prediction interval is given as

$$
[l, u]_m = n_m^* \hat{\pi} \pm q^{calib} \hat{se}(Y_m - y_m^*)
$$

where

$$
\hat{se}(Y_m - y_m^*) = \sqrt{\hat{\phi}n_m^*\hat{\pi}(1-\hat{\pi}) + \frac{\hat{\phi}n_m^* \hat{\pi}(1-\hat{\pi})}{\sum_h n_h}}
$$

with n_m^* as the number of experimental units in the future clusters, $\hat{\pi}$ as the estimate for the binomial proportion obtained from the historical data, q^{calib} as the bootstrap-calibrated coefficient, $\hat{\phi}$ as the estimate for the dispersion parameter and n_h as the number of experimental units per historical cluster.

If algorithm is set to "MS22mod", both limits of the prediction interval are calibrated independently from each other. The resulting prediction interval is given by

$$
[l, u] = \left[n_m^* \hat{\pi} - q_l^{calib} \hat{s} e(Y_m - y_m^*), \quad n_m^* \hat{\pi} + q_u^{calib} \hat{s} e(Y_m - y_m^*) \right]
$$

Please note, that this modification does not affect the calibration procedure, if only prediction limits are of interest.

Value

quasi_bin_pi returns an object of class c("predint", "quasiBinomialPI") with prediction intervals or limits in the first entry (\$prediction).

References

Menssen and Schaarschmidt (2019): Prediction intervals for overdispersed binomial data with application to historical controls. Statistics in Medicine. [doi:10.1002/sim.8124](https://doi.org/10.1002/sim.8124)

Menssen and Schaarschmidt (2022): Prediction intervals for all of M future observations based on linear random effects models. Statistica Neerlandica, [doi:10.1111/stan.12260](https://doi.org/10.1111/stan.12260)

Examples

```
# Pointwise prediction interval
pred_int <- quasi_bin_pi(histdat=mortality_HCD, newsize=40, nboot=100)
summary(pred_int)
# Pointwise upper prediction limit
pred_u <- quasi_bin_pi(histdat=mortality_HCD, newsize=40, alternative="upper", nboot=100)
summary(pred_u)
```
quasi_pois_pi 39

Please note that nboot was set to 100 in order to decrease computing time # of the example. For a valid analysis set nboot=10000.

quasi_pois_pi *Prediction intervals for quasi-Poisson data*

Description

quasi_pois_pi() calculates bootstrap calibrated prediction intervals for Poisson data with constant overdispersion (quasi-Poisson).

Usage

```
quasi_pois_pi(
 histdat,
 newdat = NULL,newoffset = NULL,
  alternative = "both",
  alpha = 0.05,
  nboot = 10000,delta_min = 0.01,
  delta_max = 10,
  tolerance = 0.001,traceplot = TRUE,
  n_bisec = 30,
  algorithm = "MS22mod"
)
```
Arguments

Details

This function returns bootstrap-calibrated prediction intervals as well as lower or upper prediction limits.

If algorithm is set to "MS22", both limits of the prediction interval are calibrated simultaneously using the algorithm described in Menssen and Schaarschmidt (2022), section 3.2.4. The calibrated prediction interval is given as

$$
[l,u]_m=n_m^*\hat{\lambda}\pm q^{calib}\sqrt{n_m^*\hat{\phi}\hat{\lambda}+\frac{n_m^{*2}\hat{\phi}\hat{\lambda}}{\sum_h n_h}}
$$

with n_m^* as the number of experimental units in the future clusters, $\hat{\lambda}$ as the estimate for the Poisson mean obtained from the historical data, q^{calib} as the bootstrap-calibrated coefficient, $\hat{\phi}$ as the estimate for the dispersion parameter and n_h as the number of experimental units per historical cluster.

If algorithm is set to "MS22mod", both limits of the prediction interval are calibrated independently from each other. The resulting prediction interval is given by

$$
[l,u]=\Big[n^*_m\hat\lambda-q_l^{calib}\sqrt{n^*_m\hat\phi\hat\lambda+\frac{n^*_m^2\hat\phi\hat\lambda}{\sum_h n_h}},\quad n^*_m\hat\lambda+q_u^{calib}\sqrt{n^*_m\hat\phi\hat\lambda+\frac{n^*_m^2\hat\phi\hat\lambda}{\sum_h n_h}}\Big]
$$

Please note, that this modification does not affect the calibration procedure, if only prediction limits are of interest.

Value

quasi_pois_pi returns an object of class c("predint", "quasiPoissonPI") with prediction intervals or limits in the first entry (\$prediction).

References

Menssen and Schaarschmidt (2022): Prediction intervals for all of M future observations based on linear random effects models. Statistica Neerlandica, [doi:10.1111/stan.12260](https://doi.org/10.1111/stan.12260)

Examples

```
#' # Historical data
qp_dat1
# Future data
qp_dat2
# Pointwise prediction interval
pred_int <- quasi_pois_pi(histdat=ames_HCD, newoffset=3, nboot=100)
summary(pred_int)
# Pointwise upper prediction
pred_u <- quasi_pois_pi(histdat=ames_HCD, newoffset=3, alternative="upper", nboot=100)
summary(pred_u)
```
rbbinom 41

Please note that nboot was set to 100 in order to decrease computing time # of the example. For a valid analysis set nboot=10000.

rbbinom *Sampling of beta-binomial data*

Description

rbbinom() samples beta-binomial data according to Menssen and Schaarschmidt (2019).

Usage

rbbinom(n, size, prob, rho)

Arguments

Details

For beta binomial data with $i = 1, \dots I$ clusters, the variance is

$$
var(y_i) = n_i \pi (1 - \pi) [1 + (n_i - 1)\rho]
$$

with ρ as the intra class correlation coefficient

$$
\rho = 1/(1 + a + b).
$$

For the sampling $(a + b)$ is defined as

$$
(a+b) = (1-\rho)/\rho
$$

where $a = \pi(a + b)$ and $b = (a + b) - a$. Then, the binomial proportions for each cluster are sampled from the beta distribution

$$
\pi_i \sim Beta(a, b)
$$

and the number of successes for each cluster are sampled to be

$$
y_i \sim Bin(n_i, \pi_i).
$$

In this parametrization $E(\pi_i) = \pi = a/(a+b)$ and $E(y_i) = n_i\pi$. Please note, that $1 + (n_i - 1)\rho$ is a constant if all cluster sizes are the same and hence, in this special case, also the quasi-binomial assumption is fulfilled.

Value

a data.frame with two columns (succ, fail)

References

Menssen M, Schaarschmidt F.: Prediction intervals for overdispersed binomial data with application to historical controls. Statistics in Medicine. 2019;38:2652-2663. [doi:10.1002/sim.8124](https://doi.org/10.1002/sim.8124)

Examples

```
# Sampling of example data
set.seed(234)
bb_dat1 <- rbbinom(n=10, size=50, prob=0.1, rho=0.06)
bb_dat1
set.seed(234)
bb_dat2 <- rbbinom(n=3, size=c(40, 50, 60), prob=0.1, rho=0.06)
bb_dat2
```
rnbinom *Sampling of negative binomial data*

Description

rnbinom() samples negative-binomial data. The following description of the sampling process is based on the parametrization used by Gsteiger et al. 2013.

Usage

```
rnbinom(n, lambda, kappa, offset = NULL)
```
Arguments

rqbinom 43

Details

The variance of the negative-binomial distribution is

$$
var(Y_i) = n_i \lambda (1 + \kappa n_i \lambda).
$$

Negative-biomial observations can be sampled based on predefined values of κ , λ and n_i : Define the parameters of the gamma distribution as $a = \frac{1}{\kappa}$ and $b_i = \frac{1}{\kappa n_i \lambda}$. Then, sample the Poisson means for each cluster

 $\lambda_i \sim Gamma(a, b_i).$

Finally, the observations y_i are sampled from the Poisson distribution

 $y_i \sim Pois(\lambda_i)$

Value

rnbinom() returns a data.frame with two columns: y as the observations and offset as the number of offsets per observation.

References

Gsteiger, S., Neuenschwander, B., Mercier, F. and Schmidli, H. (2013): Using historical control information for the design and analysis of clinical trials with overdispersed count data. Statistics in Medicine, 32: 3609-3622. [doi:10.1002/sim.5851](https://doi.org/10.1002/sim.5851)

Examples

```
# Sampling of negative-binomial observations
# with different offsets
set.seed(123)
rnbinom(n=5, lambda=5, kappa=0.13, offset=c(3,3,2,3,2))
```
rqbinom *Sampling of overdispersed binomial data with constant overdispersion*

Description

rqbinom samples overdispersed binomial data with constant overdispersion from the beta-binomial distribution such that the quasi-binomial assumption is fulfilled.

Usage

rqbinom(n, size, prob, phi)

44 rqbinom

Arguments

Details

It is assumed that the dispersion parameter (Φ) is constant for all $i = 1, \dots I$ clusters, such that the variance becomes

$$
var(y_i) = \Phi n_i \pi (1 - \pi).
$$

For the sampling $(a + b)_i$ is defined as

$$
(a+b)_i = (\Phi - n_i)/(1 - \Phi)
$$

where $a_i = \pi(a+b)_i$ and $b_i = (a+b)_i - a_i$. Then, the binomial proportions for each cluster are sampled from the beta distribution

$$
\pi_i \sim Beta(a_i, b_i)
$$

and the numbers of success for each cluster are sampled to be

$$
y_i \sim Bin(n_i, \pi_i).
$$

In this parametrization $E(\pi_i) = \pi$ and $E(y_i) = n_i \pi$. Please note, the quasi-binomial assumption is not in contradiction with the beta-binomial distribution if all cluster sizes are the same.

Value

a data.frame with two columns (succ, fail)

Examples

```
# Sampling of example data
set.seed(456)
qb_dat1 <- rqbinom(n=10, size=50, prob=0.1, phi=3)
qb_dat1
set.seed(456)
qb_dat2 <- rqbinom(n=3, size=c(40, 50, 60), prob=0.1, phi=3)
qb_dat2
```
rqpois() samples overdispersed Poisson data with constant overdispersion from the negativebinomial distribution such that the quasi-Poisson assumption is fulfilled. The following description of the sampling process is based on the parametrization used by Gsteiger et al. 2013.

Usage

rqpois(n, lambda, phi, offset = NULL)

Arguments

Details

It is assumed that the dispersion parameter (Φ) is constant for all $i = 1, \ldots I$ clusters, such that the variance becomes

$$
var(y_i) = \Phi n_i \lambda
$$

For the sampling κ_i is defined as

$$
\kappa_i = (\Phi - 1)/(n_i \lambda)
$$

where $a_i = 1/\kappa_i$ and $b_i = 1/(\kappa_i n_i \lambda)$. Then, the Poisson means for each cluster are sampled from the gamma distribution

$$
\lambda_i \sim Gamma(a_i, b_i)
$$

and the observations per cluster are sampled to be

$$
y_i \sim Pois(\lambda_i).
$$

Please note, that the quasi-Poisson assumption is not in contradiction with the negative-binomial distribution, if the data structure is defined by the number of clusters only (which is the case here) and the offsets are all the same $n_h = n_h = n$.

Value

a data.frame containing the sampled observations and the offsets

References

Gsteiger, S., Neuenschwander, B., Mercier, F. and Schmidli, H. (2013): Using historical control information for the design and analysis of clinical trials with overdispersed count data. Statistics in Medicine, 32: 3609-3622. [doi:10.1002/sim.5851](https://doi.org/10.1002/sim.5851)

Examples

```
# set.seed(123)
qp_dat1 <- rqpois(n=10, lambda=50, phi=3)
qp_dat1
# set.seed(123)
qp_dat2 <- rqpois(n=3, lambda=50, phi=3)
qp_dat2
```
summary.predint *Summarizing objects of class* predint

Description

This function gives a summary about the prediction intervals (and limits) computed with **predint**.

Usage

```
## S3 method for class 'predint'
summary(object, ...)
```
Arguments

Value

A data.frame containing the current data (if provided via newdat), the prediction interval (or limit), the expected value for the future observation, the bootstrap calibrated coefficient(s), the prediction standard error and a statement about the coverage for each future observation, if new observations were provided via newdat.

Examples

```
# Fitting a random effects model based on c2_dat1
fit <- lme4::lmer(y_ijk~(1|a)+(1|b)+(1|a:b), c2_dat1)
```
Prediction interval using c2_dat2 as future data pred_int <- lmer_pi_futmat(model=fit, newdat=c2_dat2, alternative="both", nboot=100) summary(pred_int)

#--

Please note that nboot was set to 100 in order to decrease computing time # of the example. For a valid analysis set nboot=10000.

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